## 2019 Workshop on Gravitational Waves and High-Performance Computing Geoffrey Lovelace

Geoffrey Lovelace August 19, 2019 – August 23, 2019 Day 2

# Clicker question #2.3

What does this program print?

= 1 while j < 3:</pre> j = j + 1print(j)









2 3

4

# Clicker question #2.4

• What does this program print?

```
product = 1
j = 1
while j < 3:
    product = product * j
    j = j + 1
print(product)</pre>
```



# Clicker question #2.4b

What does this program print?



# Clicker question #2.4c

• What value of x makes the program print 24?

product = 1= 1 while j < x: product = product \* j j = j + 1print(product)



• Throw darts in square

• (circle area) ÷ (square area)  $\approx$  darts in circle  $\div$ darts in square =  $\pi/4$ 

# A silly way to compute π



Courtesy wikipedia



# Monte Carlo methods

- This idea might seem silly, but it actually has a lot of uses in physics
- Monte Carlo methods: use repeated random numbers to get results
  - Min/max of functions especially functions of many variables
  - Integrals
     especially high dimensional
  - Explore probability distributions



Images courtesy Wikipedia, Apple Maps

# Monte Carlo methods

- This idea might seem silly, but it actually has a lot of uses in physics
- When we observe a gravitational wave from merging black holes...
  - What kinds of black holes made the waves?
    - Choose random parameters (masses, spins,
    - Compute the corresponding grav. wave
    - More likely to call the wave a "hit" the better it matches—vs. the last wave "hit"



GW150914: Abbott+ (2016)

# Pi Dartboard 1

## • Write a program that prints one random number between 0 and 1



### import math import random print(random.random())



# Pi Dartboard 2

- Challenge: Modify your program
  - Store the random number in a variable x
  - Store a second random number in a variable y
  - Print x and y



import math import random print(random.random())





# Pi Dartboard 2 Solution

- Challenge: Modify your program
  - Store the random number in a variable x
  - Store a second random number in a variable y
  - Print x and y

### import math import random

()

x = random.random() = random.random() print(x) print(y)





# Pi Dartboard 3

- Challenge: Modify your program
  - Compute  $x^2 + y^2$  and store it in a variable rSquared
  - Print rSquared instead of just x and y

### import math import random

x = random.random() y = random.random()

()

## print(x) print(y)





# Pi Dartboard 3 Solution

- Challenge: Modify your program
  - Compute  $x^2 + y^2$  and store it in a variable rSquared
  - Print rSquared instead of just x and y

### import math import random

x = random.random() random.random() V =

()

 $rSquared = x^{**2} + y^{**2}$ print(rSquared)





# Clicker question #2.5

• Which could be a number the program prints?







0



# Clicker question #2.5 If the dart is inside the circle,

 If the dart is inside the which could be the number printed by the program?

### import math import random x = random.random() y = random.random() rSquared = x\*\*2 + y\*\*2 print(rSquared)





More than one of ABC

O



# Pi Dartboard 4

- Challenge: Modify your program
  - Just below import random, make a new variable called "hits", set to 0
  - If rSquared < 1, add 1 to hits
  - Print hits instead of rSquared

### import math import random

x = random.random() y = random.random()

()

 $rSquared = x^{**2} + y^{**2}$ print(rSquared)





# Pi Dartboard 4 Solution

- Challenge: Modify your program
  - Just below import random, make a new variable called "hits", set to 0
  - If rSquared < 1, add 1 to hits
  - Print hits instead of rSquared

import math import random hits = 0 x = random.random() y = random.random()  $rSquared = x^{**2} + y^{**2}$ if rSquared < 1:</pre> hits = hits + 1print(hits)





# Pi Dartboard 4.5

### • Challenge: Modify your program

- Add a new variable, just below hits, called throws. Set it equal to 10.
- Add a while loop just below your new variable, throws.
  - Make a counter variable (i or j or ...) and set it equal to zero. Then make a while loop.
    While your counter variable is less than throws, each time through the while loop, add 1 to your counter variable.



- import math
  import random
- hits = 0

x = random.random()
y = random.random()

()

rSquared = x\*\*2 + y\*\*2
if rSquared < 1:
 hits = hits + 1
print(hits)</pre>





# Pi Dartboard 4.5 solution

### • Challenge: Modify your program

- Add a new variable, just below hits, called throws. Set it equal to 10.
- Add a while loop just below your new variable, throws.
  - Make a counter variable (i or j or ...) and set it equal to zero. Then make a while loop.
    While your counter variable is less than throws, each time through the while loop, add 1 to your counter variable.

import math
import random

hits = 0throws = 10

i = 0
while i < throws:
 i = i + 1</pre>

x = random.random()
y = random.random()

()

rSquared = x\*\*2 + y\*\*2
if rSquared < 1:
 hits = hits + 1
print(hits)</pre>





# Pi Dartboard 5

- Challenge: Modify your program
  - Put the code that throws the dart and sees if it hit inside a while loop, so that you throw 10 darts instead of 1 dart
  - Your print statement should still be outside the while loop

import math import random

hits = 0throws = 10

i = 0while i < throws:</pre> i = i + 1

x = random.random() = random.random()

rSquared = x\*\*2 + y\*\*2if rSquared < 1:</pre> hits = hits + 1print(hits)





# Pi Dartboard 5 Solution

- Challenge: Modify your program
  - Add a new variable, just below hits, called throws. Set it equal to 10.
  - Put the code that throws the dart and sees if it hit inside a while loop, so that you throw 10 darts instead of 1 dart

= 0

- import math import random
- hits = 0throws = 10
- while i < throws:</pre>
  - x = random.random()

()

- = random.random()
- $rSquared = x^{**2} + y^{**2}$ if rSquared < 1: hits = hits + 1i = i + 1print(hits)





• Throw darts in square

• (circle area) ÷ (square area)  $\approx$  hits  $\div$  throws =  $\pi/4$ 

• So  $\pi \approx 4^*$  (hits  $\div$  throws)

# A silly way to compute π



Courtesy wikipedia



# Pi Dartboard 6

- Finish the dartboard
  - Make a variable pi, set to 4.0 \* float(hits) / float(throws)
    - Should you do this inside or outside the while loop?
  - Print pi

- import math
- import random
- hits = 0

= 0

- throws = 10
- while i < throws:</pre>
  - x = random.random()

()

- y = random.random()
- rSquared = x\*\*2 + y\*\*2
  if rSquared < 1:
   hits = hits + 1
  i = i + 1</pre>
- print(hits)





# Pi Dartboard 6 Solution

- Finish the dartboard
  - Compute pi as 4.0 \* float(hits) / float(throws)
  - Print your pi estimate

- import math import random
- hits = 0 throws = 10
- = 0

  - $rSquared = x^{**2} + y^{**2}$ if rSquared < 1: hits = hits + 1
- pi = 4.0 \* float(hits) / float(throws) print(pi)

O

while i < throws:</pre> x = random.random() = random.random()







- The tutor won't let us run lots of darts
- So paste this into a cell in Jupyter on colab.google.com and run it
  - See what happens as you make throws 10\*\*n, n=1,2,3,4,5,6,7



## Pi Dartboard 7 import math import random

- throws = 10
- while i < throws:</pre> x = random.random() = random.random()
  - $rSquared = x^{**2} + y^{**2}$ if rSquared < 1: hits = hits + 1

pi = 4.0 \* float(hits) / float(throws)

()







### <u>https://mybinder.org/v2/gh/geoffrey444/</u> <u>NRDataExample/master</u>

# Plotting your results

# Scatter plots Lists and numpy arrays Pyplot plotting

# Scatter plots

- Data: result or output given some input
- Example: dropped marker height vs. time
- Tools to make scatter plots
  - Excel
  - Python
    - Lists of numbers
    - Computations on lists of numbers: numpy arrays
    - pyplot: makes scatter plots

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	Α	В	С	D	E	F	G	Н	1	J	К	
1	Time (s)	Height (m)		25								
2	0	2		2.5								
3	0.05	1.98775										
4	0.1	1.951		2	• • •							
5	0.15	1.88975				••	•					
6	0.2	1.804		(s)			•					
7	0.25	1.69375		<b>9</b> 1.5			•					
8	0.3	1.559		Ŭ.								
9	0.35	1.39975		, jnt					-			
10	0.4	1.216							•			
11	0.45	1.00775	-	<b>-</b>					۲			
12	0.5	0.775		0.5					•			
13	0.55	0.51775										
14	0.6	0.236										
15	0.61	0.17671		0								
16	0.62	0.11644			0	0	.2	0.4		0.6		
17	0.63	0.05519					Tin	ne (sec	conds)			
18												



 Values - ordered sets of objects, all the same type (like floats or ints)

• Operators -[], .append()

 Easily add on elements in loops with .append()

# **S**IS

x = [-2.0, -1.0, 0.0, 1.0, 2.0]y = ["Hello", "world"] z = [1, 4, 9, 16]

### z.append(25) == [1, 4, 9, 16, 25]



# Loop over ists

### for i in [1,2,3,4]: print(i\*i)

0 1 4

9

import numpy as np print(np.arange(1,5,1)) [1, 2, 3, 4]

import numpy as np myCountArray = np.arange(1,5) myList = [] for i in myCountArray: myList.append(i\*i) print(myCountArray) print(myList) [1, 2, 3, 4][1, 4, 9, 16]



# Clicker question #2.6

• What value does the program print?

### x = [1.0, 4.0, 9.0]print(x[1])



• Values - ordered sets of objects, all the same type (like floats or ints)

• Operators - [], +, -, \*, /, np.sqrt(), np.sin(), np.cos(),

 Easily do math on whole lists at once (like formulas in Excel)



 $\times [0] == -2.0$ x[1] == -1.0x[4] == 2.0y[0] == "Hello"y[-1] == "world"z[-1] == 16z[0] == 1

# Numpy arrays

x = np.array([-2.0, -1.0, 0.0, 1.0, 2.0])y = np.array(["Hello", "world"]) q = np.array([1, 2, 3, 4])r = q \* 2

s = q + rz = q \* q

> r == np.array([2, 4, 6, 8]) s == np.array([3, 6, 9, 12]) z == np.array([1, 4, 9, 16])



# Naking sample data

- Annoying to type [1,2,3,4,...] all the time
- Instead: np.arange(start, stop, step)
- What do all these numbers mean??
  - Make a plot to visualize them

## Try in colab!

import numpy as np x = np.arange(-4.0, 4.0, 0.01)y = np.sin(x) \*\*3print(x) print(y)

-9.99825171e-01-9.99351433e-01-9.98578166e-01-9.97505912e-01
-9.96135421e-01-9.94467651e-01-9.92503769e-01-9.90245148e-01
-9.87693366e-01-9.84850205e-01-9.81717651e-01-9.78297888e-01
-9.74593301e-01-9.70606471e-01-9.66340175e-01-9.61797379e-01
-9.56981241e-01-9.51895105e-01-9.46542499e-01-9.40927131e-01
-9.35052889e-01-9.28923832e-01-9.22544191e-01-9.15918365e-01
-9.09050915e-01 -9.01946561e-01 -8.94610179e-01 -8.87046794e-01
-8.79261581e-01 -8.71259853e-01 -8.63047062e-01 -8.54628794e-01
-8.46010761e-01-8.37198799e-01-8.28198860e-01-8.19017011e-01
-8.09659425e-01-8.00132377e-01-7.90442239e-01-7.80595473e-01
-7.70598629e-01 -7.60458333e-01 -7.50181290e-01 -7.39774268e-01
-7.29244102e-01 -7.18597680e-01 -7.07841944e-01 -6.96983877e-01
-6.86030504e-01-6.74988880e-01-6.63866088e-01-6.52669231e-01
-6.41405427e-01-6.30081800e-01-6.18705479e-01-6.07283586e-01
-5.95823237e-01-5.84331527e-01-5.72815532e-01-5.61282298e-01
-5.49738839e-01-5.38192126e-01-5.26649084e-01-5.15116589e-01
-5.03601455e-01-4.92110435e-01-4.80650212e-01-4.69227393e-01
-4.57848505e-01-4.46519990e-01-4.35248195e-01-4.24039375e-01
-4.12899678e-01-4.01835147e-01-3.90851715e-01-3.79955193e-01
-3.69151273e-01 -3.58445520e-01 -3.47843366e-01 -3.37350109e-01
-3.26970907e-01-3.16710771e-01-3.06574566e-01-2.96567003e-01
-2.86692639e-01 -2.76955868e-01 -2.67360924e-01 -2.57911871e-01



# Plotting sample data Try in colab!

Make plots with pyplot

import numpy as np import matplotlib from matplotlib import pyplot as plt matplotlib.rc('axes', labelsize=18) matplotlib.rc('xtick', labelsize = 18) matplotlib.rc('ytick', labelsize = 18)

x = np.arange(-4.0, 4.0, 0.01)
y = np.sin(x)\*\*3

plt.clf() #clear figure
plt.plot(x,y, color='b')
plt.xlabel('x')
plt.ylabel('sin^3(x)')
plt.show()





Х

# Functions

- Input(s) ("arguments")
- Returns output
- Functions can call other functions

### Try in tutor! def square(x): return x\*x square(4) 16
## 

#### • Activity: edit your code

- Make everything but the first two lines and last two lines inside a function that takes one input, throws
- Instead of setting throws = 10, throws in an input to the function
- Return the pi estimate
- Have your print statement just use your function



#### import math import random

- while i < throws:</pre>
  - x = random.random()
    - = random.random()
  - $rSquared = x^{**2} + y^{**2}$ if rSquared < 1:</pre> hits = hits + 1= i + 1

= 4.0 \* float(hits) / float(throws)



### Solution

#### • Activity: edit your code

- Make everything but the last two lines inside a function that takes one input, n
- Instead of setting throws = 10, set throws=n
- Return the pi estimate

#### import math import random

i = 0

pi = 4.0 \* float(hits) / float(throws) return pi

```
def estimatePi(throws):
  hits = 0
  while i < throws:</pre>
      x = random.random()
      y = random.random()
```

 $rSquared = x^{**2} + y^{**2}$ if rSquared < 1:</pre> hits = hits + 1i = i + 1

print(estimatePi(le4))



## Potting m 2

#### Activity: edit your code

- Make a list of different numbers of throws: 10, 100, 1000, ... up to 1e7
- Make an empty list called piEstimates
- Loop over the list you made, estimating  $\pi$  for different numbers of throws

import math import random

return pi

print(estimatePi(1e4))



#### def estimatePi(throws): # (same definition of estimatePi function here)



## Plotting π solution 2

#### Activity: edit your code

- Make a list of different numbers of throws: 10, 100, 1000, ... up to 1e7
- Make an empty list called piEstimates
- Loop over the list you made, estimating  $\pi$  for different numbers of throws

import math import random

def estimatePi(throws): # (same definition of estimatePi function here) return pi

throwsList = [1e1, 1e2, 1e3, 1e4, 1e5, 1e6, 1e7] piEstimatesList = [] for throws in throwsList: piEstimatesList.append(estimatePi(throws)) print(piEstimatesList)







## Potting m 3

- Activity: edit your code
  - Don't print piEstimatesList
  - Instead, make a scatter plot of throwsList vs. piEstimatesList
  - Use a log scale on the x axis: plt.xscale('log')

import math import random

def estimatePi(throws): # (same definition of estimatePi function here) return pi

throwsList = [1e1, 1e2, 1e3, 1e4, 1e5, 1e6, 1e7] piEstimatesList = [] for throws in throwsList: piEstimatesList.append(estimatePi(throws)) print(piEstimatesList)





### Solution 3

- Activity: edit your code
  - Don't print piEstimatesList
  - Instead, make a scatter plot of throwsList vs. piEstimatesList
  - Use a log scale on the x axis: plt.xscale('log')

import math import random import matplotlib

def estimatePi(throws): # (same definition of estimatePi function here) return pi

plt.clf() plt.show()

```
import numpy as np
from matplotlib import pyplot as plt
matplotlib.rc('axes', labelsize=18)
matplotlib.rc('xtick', labelsize = 18)
matplotlib.rc('ytick', labelsize = 18)
```

```
throwsList = [1e1, 1e2, 1e3, 1e4, 1e5, 1e6, 1e7]
piEstimatesList = []
for throws in throwsList:
    piEstimatesList.append(estimatePi(throws))
```

```
plt.plot(throwsList, piEstimatesList)
plt.xlabel('Number of throws')
plt.xscale('log')
plt.ylabel('Estimate of pi')
```



### Accuracy of the $\pi$ dart board

- As throws goes up, answer gets closer to pi
- But it's hard to see how close it is later on
- So instead, plot the difference between the estimate and the real answer

Estimate of pi 3.2

3.6



## Potting π4

- Challenge: edit your code
  - import numpy as np
  - piEstimates = np.array(piEstimatesList)
  - Plot throwsList vs. abs(piEstimates - math.pi)
  - Put y axis on a log scale
  - Update y axis label to be abs(estimate of pi - pi)

plt.clf() plt.show()

#### # ... code that computes pi

```
throwsList = [1e1, 1e2, 1e3, 1e4, 1e5, 1e6, 1e7]
piEstimatesList = []
for throws in throwsList:
    piEstimatesList.append(estimatePi(throws))
plt.plot(throwsList, piEstimatesList)
plt.xlabel('Number of throws')
plt.xscale('log')
plt.ylabel('Estimate of pi')
```



### Solution 4

- Challenge: edit your code
  - import numpy as np
  - piEstimates = np.array(piEstimatesList)
  - Plot throwsList vs. abs(piEstimates - math.pi)
  - Put y axis on a log scale
  - Update y axis label to be abs(estimate of pi - pi)

plt.clf() plt.xscale('log') plt.yscale('log') plt.show()

#### # ... code that computes pi

```
throwsList = [1e1, 1e2, 1e3, 1e4, 1e5, 1e6, 1e7]
piEstimatesList = []
```

- **for** throws **in** throwsList:
  - piEstimatesList.append(estimatePi(throws))

```
piEstimates = np.array(piEstimatesList)
plt.plot(throwsList, abs(piEstimates - math.pi))
plt.xlabel('Number of throws')
plt.ylabel('abs(Estimate of pi - pi)')
```

pi - pi)	10 <sup>-1</sup>	
s(Estimate of	10 <sup>-2</sup>	
	10 <sup>-3</sup>	
ab	10 <sup>-4</sup>	
		102



# Concepts in numerical programming

#### Resolution

Accuracy

Precision



## Resolution

#### Low resolution Entire image: 227KB

*Large galaxies* 1 *billion light years away* 

Small galaxies up to 13 billion light years away

Image courtesy NASA





#### High resolution Entire image: 110MB

*Large galaxies* 1 *billion light years away* 

Small galaxies up to 13 billion light years away

Image courtesy NASA

## Resolution



### Resolution

#### Low resolution

- Smaller data
- Faster computation
- Less precise
- High resolution
  - Bigger data
  - Slower computation
  - More precise







#### Precision

- How much result changes when you add more resolution
- "How many digits"

#### Accuracy

 How close result is to the correct result



### Example: thermal noise

 Thermal noise of a mirror in LIGO depends on how much potential energy it gets when you push on the face



Color = how much mirror deforms



Lovelace, Demos, Khan (2018)



### Example: thermal noise

- Potential energy *E* in deformed mirror
  - Precision of energy as resolution increases
    - Label resolution by integer N



#### AlGaAs (effective isotropic)

Higher resolution

Lovelace, Demos, Khan (2018)



### Example: thermal noise

- Thermal noise of thin coating
  - Accuracy: compare code to known "analytic" solution



Lovelace, Demos, Khan (2018)



### Unix terminal on the web

### NRDataExample/master

Choose "New Terminal"

Go to <u>https://mybinder.org/v2/gh/geoffrey4444/</u>

of throws. The horizontal axis shows



### Your graph plots abs(estimate of pi - pi) vs number

of throws. The vertical axis shows



### Your graph plots abs(estimate of pi - pi) vs number



#### • As the number of throws increases, the resolution



#### • As the number of throws increases, the accuracy

### Example: π dart board

- Need roughly 100x
   more darts to get 10x
   more accuracy
  - That is, 100x darts gives you 10x more accuracy
  - This gets slow fast!
  - Can we do better?

pi - pi)	10 <sup>-1</sup>	
late of	10 <sup>-2</sup>	
s(Estim	10 <sup>-3</sup>	
ab	10 <sup>-4</sup>	





### Connect to ocean (use our laptops)

- Open "PuTTY 64-bit" on the desktop
- Under "saved sessions" select "ocean"
- Click "Open"
- Username: workshopStudents2019
- Passphrase
  - Some computers: workshop2019!!
- squeue
- /bin/bash

• srun -p orca-1 --nodes=1 --tasks-per-node=20 --pty



### UNIX command line crash course activity

- Commands to know
  - Is, pwd, cd, mkdir
  - ./, ../, paths
  - cp, mv, rm, rmdir
  - cat, less
  - nano
  - whoami, date, ...

- Play along with me...
  - mkdir YOURNAME and cd into it
  - Navigate file system: Is, pwd, cd, ./ and ../
  - Use nano to write a text file
  - Copy, rename, remove a file
  - Cat, less, more, head, tail
  - > to redirect output
  - Grab bag: whoami, date, grep, sed, zip...

### Unix commands to know

- Commands to know
  - Is, pwd, cd, mkdir
  - ./, ../, paths
  - cp, mv, rm, rmdir
  - cat, less
  - nano
  - whoami, date, ...

- Play along with me...
  - mkdir YOURNAME and cd into it
  - Navigate file system: Is, pwd, cd, ./ and ../
  - Use nano to write a text file
  - Copy, rename, remove a file
  - Cat, less, more, head, tail
  - > to redirect output
  - Grab bag: whoami, date, grep, sed, man,

command would I use?

S

CC



### • I want to list the files in the directory I'm in. Which



pwd

#### nano

• Which command edits the file "Hello.txt" in the directory I am currently in?

nano ./Hello.txt

cat ./Hello.txt





#### nano ../Hello.txt

cat ../Hello.txt

 Which command makes a new directory called "TestFolder"?





#### Is TestFolder

#### cd TestFolder



#### mkdir TestFolder

cp TestFolder

- directory, which is not empty?
  - rmdir ./
  - rm -r ./\*
  - rm -r . /\*

More than one of these will work



• Which command removes everything in the current

- Commands to know
  - Is, pwd, cd, mkdir
  - ./, ../, paths
  - cp, mv, rm, rmdir
  - cat, less
  - nano
  - whoami, date, ...

### Unix activity

• Use nano to write a bash script (each line is a command like you would enter on the command line)

• The script should...

- Print the current date and time
- Print the current directory
- Copy /proc/cpuinfo into the current directory
- Get the first line of the copied file, and save it to a file called FirstLineOfProc.txt
- Bonus: Use grep to only show the line with "cpu cores"
- Bonus: use sed to remove all but the core number
- Bonus: instead of copying the /proc/cpuinfo file, copy whatever file users specify as an argument (google bash arguments)



### Parallel computing

- Supercomputers have lots of cores
- But each core is not much faster than a PC
- To take full advantage, you have to write code that can run on more than one core at the same time
  - That is, code that runs in parallel



#### Image courtesy Blue Waters



### Connect to ocean

- Open "PuTTY 64-bit" on the desktop
- Under "saved sessions" select "ocean"
- Click "Open"
- Username: workshopStudents2019
- Passphrase
  - Some computers: workshop2019!!
- squeue
- /bin/bash

• srun -p orca-1 --nodes=1 --tasks-per-node=20 --pty

## Parallel computing 1

- Log into ocean
- Do this

#Replace GeoffreyLovelace with YourName cd student folders mkdir YOUR NAME #replace with your lastName firstName cd YOUR NAME

mkdir PiDart cd PiDart source /opt/ohpc/pub/apps/anaconda2/bin/activate root

## Parallel computing 2

#### •nano Hello.py

#### print("Hello")

•mpirun -np 8 python Hello.py

•What happens? What happens if you change 8 to another number less than 8?
## What happened?

- mpirun ran many copies of "Hello.py"
- Each copy printed "Hello"
  - But the processors are not working together yet, or even doing anything different
- Next: make different processors do different things

## Parallel computing 3

- cp Hello.py MpiHello.py
- •nano MpiHello.py

from mpi4py import MPI comm = MPI.COMM WORLDrank = comm.Get rank() size = comm.Get size() "+str(size))

• mpirun -np 4 python MpiHello.py

•mpirun -np 8 python MpiHello.py

## print("Hello from processor "+str(rank)+" out of